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FAKULTÄT  
FÜR MATHEMATIK, INFORMATIK  
UND NATURWISSENSCHAFTEN

Fachbereich Mathematik

# Kolloquium über Mathematische Statistik und Stochastische Prozesse

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**16.01.2018, 16:15 Uhr, Hörsaal 5**

## **Scoring rules and forecast evaluation**

Abstract:

Abstract: Scoring functions and rules are essential tools for forecast evaluation and also for estimation, and we start with an overview of some more recent results which illustrate their use in these regards. In the main part of the talk we discuss weighted scoring rules for forecast evaluation and their connection to hypothesis testing. First, a general construction principle for strictly locally proper weighted scoring rules based on conditional densities and scoring rules for probability forecasts is proposed. We show how likelihood-based weighted scoring rules from the literature fit into this framework, and also introduce a weighted version of the Hyvärinen score, which is a local scoring rule in the sense that it only depends on the forecast density and its derivatives at the observation, and does not require evaluation of integrals. Further, we discuss the relation to hypothesis testing. Using a weighted scoring rule introduces a censoring mechanism, in which the form of the density is irrelevant outside the region of interest. For the resulting testing problem with composite null - and alternative hypotheses, we construct optimal tests, and identify the associated weighted scoring rule. As a practical consequence, using a weighted scoring rule allows to decide in favor of a forecast which is superior to a competing forecast on a region of interest, even though it may be inferior outside this region. A simulation study and an application to financial time-series data illustrate these findings.

References: Holzmann, H., Klar, B. (2017) Focusing on regions of interest in forecast evaluation. to appear: Annals of Applied Statistics

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<https://www.uni-marburg.de/fb12/kooperationen/stoch/personal/holzmann/index.html>

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